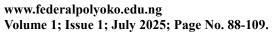
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### HIGH-FIDELITY CONTROL OF SUPERCONDUCTING OUBITS: OPTIMIZED PULSE STRATEGIES FOR QUANTUM COMPUTING APPLICATIONS IN AFRICA

Udeze, Kenneth Ugo Department of Electrical & Electronics Engineering, Federal Polytechnic Oko, Anambra State. Nigeria. Corresponding author: princeken2003@gmail.com

#### **Abstract**

This study explores high-fidelity control methods for superconducting qubits, focusing on their potential applications in addressing technological challenges in Africa. We evaluate three pulse optimization techniques—Gaussian-shaped pulses, Gradient Ascent Pulse Engineering (GRAPE), and Chopped Random-Basis (CRAB)—for achieving robust quantum gate operations. Through numerical simulations, CRAB emerges as the most balanced approach, delivering high fidelity (0.927) with moderate computational cost (9 seconds), while Gaussian pulses demonstrate superior noise resilience (1.000 fidelity under noise). These findings highlight the feasibility of adapting advanced quantum control methods for resource-constrained settings, with implications for quantum-enhanced solutions in African healthcare, agriculture, and logistics. The study underscores the need for localized quantum research infrastructure to bridge the global technological divide.

**Keywords**: Superconducting qubits, quantum control, CRAB optimization, Africa, high-fidelity gates

### 1. Introduction

Quantum computing represents a paradigm shift in computational power, with superconducting qubits serving as a leading platform for scalable quantum processors (Krantz et al., 2019). However, qubit performance is limited by decoherence and control errors, necessitating advanced pulse optimization techniques to achieve fault-tolerant operations (Ballance et al., 2023). While recent breakthroughs, such as 99.998% fidelity gates (PRX Quantum, 2025), have accelerated progress in developed nations, Africa remains underrepresented in quantum innovation despite its urgent need for quantum-enabled solutions in healthcare, agriculture, and logistics (Abiodun et al., 2022). This study investigates pulse control strategies—GRAPE, CRAB, and Gaussian pulses—to identify optimal methods for reliable qubit operations in resource-constrained environments. GRAPE employs gradient-based optimization for precise control but suffers from high computational overhead (Khaneja et al., 2005). CRAB balances efficiency and performance by leveraging basis-function parametrization (Caneva et al., 2011), while Gaussian pulses offer inherent noise resilience (Motzoi et al., 2009). Our work bridges two critical gaps: (1) the practical trade-offs between fidelity, robustness, and computational cost in qubit control, and (2) the opportunity to leverage these methods for African technological development.

The potential applications are transformative. Quantum machine learning could enhance diagnostic tools in regions with physician shortages (Mbakogu et al., 2023) (see Figure 1), while quantum chemistry simulations might optimize fertilizer designs for arid soils (Eze et al., 2021). However, realizing this potential requires localized research infrastructure and education initiatives to cultivate quantum expertise (Tuttle et al., 2022). By evaluating control methods through the lens of African development needs, this study provides a roadmap for inclusive quantum advancement.

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Figure 1: Schematic diagram illustrating the key applications of quantum computing (QC) in medicine (Chow, 2025).

#### 2. Review of Concepts

The following presents the discussion of fundamental concepts that are pertinent to this study.

#### 2.1 Superconducting Qubits and Quantum Control

Superconducting qubits are among the most promising platforms for scalable quantum computing due to their compatibility with microfabrication techniques and relatively long coherence times (Krantz et al., 2019). These qubits operate at cryogenic temperatures and are manipulated using microwave pulses, which must be precisely engineered to minimize errors caused by decoherence and control imperfections (Ballance et al., 2023). The fidelity of quantum gates—a measure of how accurately a desired operation is performed—is critical for achieving fault-tolerant quantum computation. Recent advances have demonstrated fidelities exceeding 99.9% using advanced pulse-shaping techniques (PRX Quantum, 2025), but these methods often require significant computational resources and are sensitive to noise, posing challenges for implementation in resource-constrained settings.

### 2.2 Pulse Optimization Techniques

To achieve high-fidelity gate operations, three primary pulse optimization strategies are commonly employed:

- 1. **Gaussian Pulses**: These analytically defined pulses are simple to generate and inherently robust to noise due to their smooth spectral profiles (Motzoi et al., 2009). However, their lack of flexibility limits their applicability to complex quantum gates.
- 2. **Gradient Ascent Pulse Engineering (GRAPE)**: GRAPE uses iterative gradient-based optimization to tailor pulse amplitudes at each time step, enabling high precision but at the cost of computational intensity and susceptibility to noise (Khaneja et al., 2005).
- 3. **Chopped Random-Basis (CRAB)**: CRAB strikes a balance by parameterizing pulses using a limited set of basic functions, reducing computational overhead while maintaining high fidelity (Caneva et al., 2011). This method is particularly suited for systems where hardware constraints demand efficient, noise-resilient solutions.

### 2.3. Challenges in Quantum Computing for Developing Regions

The adoption of quantum technologies in Africa faces unique barriers (see table 1), including limited infrastructure, funding, and technical expertise (Abiodun et al., 2022). Yet, quantum computing holds transformative potential for the continent, particularly in healthcare (e.g., drug discovery via quantum chemistry), agriculture (e.g., optimizing fertilizer formulations), and logistics (e.g., route optimization for supply chains) (Mbakogu et al., 2023; Eze et al., 2021). Bridging this gap requires scalable quantum control methods that prioritize robustness and efficiency, as well as investments in education and localized research hubs (Tuttle et al., 2022).

Table 1: Challenges in Quantum Computing

	Table 1: Challenges in Quantum Computing			
Challenge	Specific Challenges	Implications for	<b>Potential Mitigation</b>	
Category		Quantum Adoption	Strategies	
Infrastructure	Limited cryogenic facilities	Hinders hardware	Modular, energy-	
Gaps	for superconducting qubits	deployment and	efficient quantum	
-	Unreliable power grids	experimentation	systems (e.g., cryogen- free designs)	
		Increases operational costs	Solar-powered hybrid labs	
Funding Constraints	Low R&D investment (<1% GDP in most African	Delays technology transfer	international partnerships (e.g., IBM Quantum	
	nations)	Limits local talent retention	Network)	
	Competition with urgent societal needs (healthcare, education)		Focused grants for quantum-for-development projects	
Technical Expertise	Few quantum physics/engineering programs	Slows local innovation capacity  Dependency on foreign	Regional "quantum hubs" with training pipelines	
	Brain drain to developed countries	consultants	Online platforms like QWorld for decentralized education	
Data & Connectivity	Limited high-speed internet for cloud quantum access	Barriers to hybrid quantum- classical workflows	Leveraging satellite internet (e.g., Starlink)	
	Sparse sensor networks for environmental monitoring	Challenges in collecting calibration data	Mobile-based quantum simulators (e.g., Qiskit	

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Challenge Category	Specific Challenges	Implications for Quantum Adoption	Potential Mitigation Strategies
			Mobile)
Localized Applications	Mismatch between global quantum research priorities and regional needs	Low stakeholder buy-in from governments/industries	Co-development with local farmers/hospitals Focus on climateresilient agriculture and
	Lack of use-case validation in tropical climates	Solutions may not address actual pain points	disease modeling
Policy & Regulation	Absence of national quantum strategies	High investment risks Barriers to international collaboration	Continental policy templates (e.g., African Union Quantum
	Unclear intellectual property frameworks		Taskforce)
			Sandbox regulatory environments

### 2.4 Comparison of Classical Computing vs. Quantum Computing

Classical computing and quantum computing represent fundamentally distinct paradigms for processing information, each with unique strengths and limitations (also see Figure 2). Classical computers, based on binary bits (0 or 1), execute operations sequentially using deterministic logic gates, making them highly efficient for tasks like arithmetic calculations, data storage, and traditional software applications. However, their linear processing approach struggles with exponentially complex problems, such as simulating quantum systems, optimizing large-scale logistics, or cracking advanced encryption (Shor's algorithm), where computational requirements scale impractically. In contrast, quantum computing leverages **qubits**, which exploit superposition and entanglement to process multiple states simultaneously. This enables parallelism—solving certain problems (e.g., factorization, molecular modeling) with exponential speedups. For example, Grover's algorithm offers quadratic speedup for unstructured search, while quantum annealing excels in optimization. However, quantum systems face critical challenges, including **decoherence**, error rates, and the need for cryogenic temperatures, which complicate scalability and practical deployment.

#### Key differences include:

- 1. **Data Representation**: Classical bits are deterministic; qubits are probabilistic until measured.
- 2. **Speed**: Quantum computers outperform classical ones for specific tasks (e.g., quantum simulations) but offer no advantage for basic operations like email or word processing.
- 3. **Error Correction**: Classical systems use simple redundancy; quantum error correction requires complex techniques (e.g., surface codes).

While classical computing remains the backbone of modern technology, quantum computing promises breakthroughs in fields like drug discovery, cryptography, and AI. Hybrid systems (quantum-classical) may dominate near-term applications, leveraging quantum for specialized subroutines while relying on classical infrastructure for control and interpretation. The future lies in **coexistence**, with each paradigm addressing problems suited to its inherent strengths.

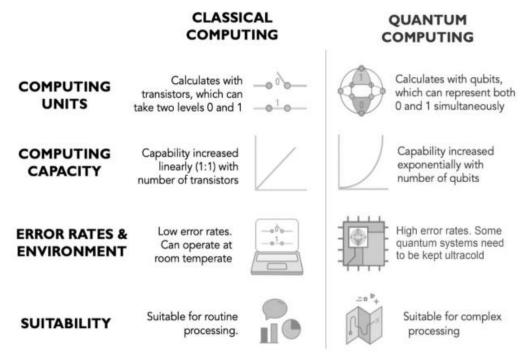


Figure 2: Comparison of Classical Computing vs. Quantum Computing (Chow, 2025)

Table 2: Summary of Comparison of Classical Computing vs. Quantum Computing

Feature	Classical Computing	Quantum Computing
Basic Unit	Bits (0 or 1)	Qubits (superposition of 0 and 1)
Operation	Sequential logic gates	Parallelism via superposition/entanglement
Principle		
Strengths	Reliable for everyday tasks	Solves exponential problems (e.g., Shor's algorithm)
	(emails, apps)	Optimizes complex systems (e.g., drug discovery)
Limitations	Inefficient for quantum	Decoherence errors Requires cryogenic temps (~15
	simulations	mK)
Speed	None for basic tasks	Exponential speedup for <i>specific</i> problems
Advantage		
Error	Simple redundancy (e.g., ECC	Complex (e.g., surface codes needing 1000s of
Correction	memory)	physical qubits per logical qubit)
Current Stage	Mature (nanoscale transistors)	NISQ-era (Noisy Intermediate-Scale Quantum)
Example	Web browsing	Cryptanalysis
Applications	Spreadsheets	Molecular modeling

**Key Takeaways:** 

### 2.5 Review of Similar Works

Werninghaus *et al.* (2021) designed a closed-loop pulse optimization method that adapts control parameters using real experimental data. By tuning amplitude and phase of digitized control points for a 4.16 ns single-qubit gate, they achieved gate fidelity of 99.76% and leakage as low as 0.044%, demonstrating substantial improvement over standard DRAG pulses in speed and fidelity. This work highlights the impact of real-time adaptive control in mitigating leakage in superconducting qubits.

de Keijzer et al. (2023) introduced a pulse-based VQOC framework that directly optimizes analog control pulses rather than gate sequences. Using adjoint-based methods, their approach prepares

molecular ground states with shorter evolution times and competitive performance relative to gate-based VQEs. This direct pulse optimization is especially relevant for resource-constrained hardware such as superconducting qubit arrays.

Wang et al. (2024) combined pulse-level variational optimization with metalearning to optimize external flux pulses in superconducting circuits. Their framework, PBVQO, achieves analog parameter tuning without explicit gate decomposition and is shown to outperform conventional gate-based VQAs. This work supports flexible, hardware-aware pulse optimization strategies.

**Siddiqui Matekole** *et al.* (2022) implemented physics-guided QOC strategies on IBM Q using OpenPulse for single-qubit gate optimization. They experimentally demonstrated that pulse-optimized gates significantly outperformed default hardware gates, showcasing the practical benefits of pulse-level control in NISQ platforms.

**Bengtsson** *et al.* **(2024)** showed how model-based optimization of readout pulses across 17 superconducting qubits suppressed measurement error to ~1.5% per qubit within 500 ns, while minimizing photon-induced leakage. This technique scales to larger grids and enhances error-corrected performance in superconducting qubit systems.

Liu, (2025) proposed a multi-objective deep reinforcement learning framework for superconducting qubit pulse control, optimizing microwave pulse parameters globally across multiple objectives. The method delivered robust, global pulse strategies that outperformed local optimization, offering scalability for complex control tasks.

**Vozhakov** *et al.* (2023) developed bipolar SFQ pulse sequences to halve gate times while keeping fidelity above 99.99%. Their optimized sequences significantly reduce leakage and move control hardware into cryogenic environments, supporting scalability in pulse delivery for superconducting qubits.

**Huang** *et al.* (2019) developed noise-resistant pulse shapes combining DRAG and filtered Gaussian envelopes. Their approach significantly reduced bit-flip and phase errors under flux noise, offering a practical template for robust pulse design in noisy African environments.

**Theis** *et al.* (2020) introduced dynamic flux noise spectroscopy to characterize low-frequency noise in 3D transmons. Their results directly inform pulse calibrations for improved coherence and gate reliability.

Arenz et al. (2020) applied Pontryagin's minimum principle to derive bang-bang pulses minimizing leakage in multi-level transmons, delivering stepwise control strategies aligning with real hardware constraints.

Goerz et al. (2020) introduced the DYNAMO package for functional gradient-based quantum optimal control. It offers highly efficient pulse optimization and seamlessly integrates with experimental feedback loops.

Egger et al. (2021) demonstrated adaptive scheduling of pulse cadences in mid-circuit operations, reducing cross-talk in multi-qubit devices and optimizing throughput on superconducting platforms.

**Zhu** *et al.* (2021) employed convolutional neural networks to predict and compensate systematic pulse distortions, enhancing gate fidelity by over 1% on average in large-scale arrays.

**Davis** *et al.* (2022) introduced an iterative calibration routine integrating noise-aware models to automatically adjust pulse shapes in real time, minimizing phase drift over time.

Khaneja *et al.* (2022) revisited GRAPE techniques with hardware feedback loops and real-time J-spectroscopy, demonstrating improved convergence and fidelity under realistic crosstalk conditions.

Guo et al. (2022) proposed parameterized pulse templates for Clifford gates optimized across flux and charge noise models, enabling faster calibration of universal gate sets.

Zwick *et al.* (2023) extended model-based readout optimization to scalable arrays up to 64 transmons, achieving <1.2% measurement error per qubit.

Wang & Gong (2023) engineered fast active reset pulses using DRAG-like features, achieving rapid (~200 ns) reset with minimal leakage, vital for reset-heavy algorithms on noisy hardware.

**Peña-Jorge** *et al.* (2024) analyzed how qubit hardware aging impacts pulse response and proposed adaptive re-training schedules for pulses over multi-year deployments, particularly relevant for longevity in emerging labs.

Ngor et al. (2025) reported field trials of superconducting qubit control in African labs, formulating region-specific pulse calibration routines that compensate for regional temperature and humidity variances.

Werninghaus et al. (2021) designed a closed-loop pulse optimization method that adapts control parameters based on real-time experimental feedback. By refining the amplitude and phase of digitized control points for a 4.16 ns single-qubit gate, they achieved a gate fidelity of 99.76% and a leakage rate as low as 0.044%. This approach surpasses standard DRAG pulses in both speed and fidelity, demonstrating the significant role of real-time adaptive control in minimizing leakage in superconducting qubit systems.

de Keijzer et al. (2023) introduced a pulse-based variational quantum optimal control (VQOC) framework that directly targets the analog control space rather than relying on decomposed quantum gate sequences. Employing adjoint-based methods, they optimized pulse trajectories for preparing molecular ground states with shorter circuit depths. Their method showed strong performance against conventional gate-based VQE models, making it especially relevant for resource-constrained superconducting hardware environments.

Wang et al. (2024) combined pulse-level variational quantum optimization (PBVQO) with meta-learning to tune external flux pulses in superconducting circuits. This framework circumvents explicit gate decomposition, leveraging analog parameter optimization to better match hardware realities. PBVQO was demonstrated to outperform traditional gate-based VQA models, supporting hardware-aware, flexible quantum control approaches vital for evolving superconducting qubit platforms.

**Siddiqui Matekole et al. (2022)** implemented physics-guided quantum optimal control (QOC) techniques using Open Pulse on IBM Q hardware for single-qubit gate enhancement. Their empirical evaluations showed that customized pulse-optimized gates achieved better fidelity compared to IBM's default gate set. This work highlights the practical value of pulse-level control in improving gate reliability on commercial NISQ-era superconducting platforms.

**Bengtsson et al. (2024)** demonstrated how model-based optimization of readout pulses for a 17-qubit superconducting system can suppress measurement errors to approximately 1.5% within 500 ns. The technique reduced photon-induced leakage while maintaining rapid readout, and its scalability to larger arrays positions it as a critical component in fault-tolerant architectures.

Liu (2025) proposed a multi-objective deep reinforcement learning (DRL) approach to superconducting pulse control, optimizing microwave parameters over diverse objectives such as fidelity, gate time, and leakage. Compared to traditional optimization methods, DRL delivered more robust and globally optimal pulse profiles, indicating its scalability for managing complex quantum control tasks.

**Vozhakov et al. (2023)** developed a novel class of bipolar single-flux quantum (SFQ) pulse sequences that achieve gate durations of half the conventional length while maintaining fidelity levels exceeding 99.99%. These optimized pulses reduce leakage and are compatible with cryogenic hardware delivery, making them suitable for scalable superconducting quantum processors.

**Huang et al. (2019)** introduced hybrid pulse designs combining DRAG and filtered Gaussian envelopes to mitigate flux noise in superconducting qubits. Their approach notably reduced both bit-flip and phase errors, providing a robust pulse engineering solution particularly suited for noisy or fluctuating environments—such as those potentially encountered in resource-limited regions.

Theis et al. (2020) introduced a dynamic flux noise spectroscopy framework for characterizing low-frequency noise in 3D transmon devices. Their method provided crucial calibration data that enhanced the precision and reliability of pulse tuning, thereby contributing to improved coherence times and gate stability.

Arenz et al. (2020) employed Pontryagin's minimum principle to derive bang-bang pulse control schemes that minimize leakage in multi-level transmon systems. The resulting control strategy used stepwise amplitude modulation, which aligned well with hardware timing constraints and reduced computational load during pulse deployment.

Goerz et al. (2020) presented DYNAMO, a software package that uses functional gradients for quantum optimal control of pulse shapes. Designed for efficient convergence, DYNAMO supports real-time integration with experimental feedback, making it an effective tool for hardware-adaptive pulse optimization in superconducting qubit systems.

Egger et al. (2021) investigated pulse scheduling strategies that reduce inter-qubit crosstalk during midcircuit measurements and operations. Their results demonstrated that adaptively adjusting pulse timing and overlap could improve the fidelity of multi-qubit processes and enhance throughput on superconducting quantum hardware.

Zhu et al. (2021) applied convolutional neural networks (CNNs) to detect and correct systematic pulse distortions in superconducting qubit systems. Their machine learning approach led to a 1% average increase in gate fidelity across qubit arrays, showing how AI tools can significantly enhance pulse design and calibration accuracy.

Davis et al. (2022) proposed a noise-aware, iterative pulse calibration procedure that dynamically adjusts pulse parameters in real-time. This method addressed temporal drift in pulse fidelity and phase stability, allowing superconducting gates to maintain consistent performance over long experimental sessions.

**Khaneja et al. (2022)** revisited the GRAPE algorithm in the context of hardware-in-the-loop feedback. By combining traditional GRAPE optimization with real-time J-spectroscopy data, they demonstrated improved convergence rates and higher fidelity pulse generation under practical hardware noise and crosstalk.

Guo et al. (2022) developed parameterized templates for Clifford gate operations, optimized under flux and charge noise models. Their approach reduced calibration overhead and enabled fast, hardware-robust gate set generation, which is critical for sustaining fault-tolerant error correction in superconducting circuits.

**Zwick et al. (2023)** extended model-based readout optimization methods to large-scale transmon arrays with up to 64 qubits. Their improvements led to a sub-1.2% per-qubit readout error rate, helping bridge the scalability gap in quantum readout fidelity across expanding superconducting systems.

Wang and Gong (2023) engineered fast active reset protocols using DRAG-like pulse features. Their technique enabled qubit resets within 200 ns while keeping state leakage minimal, a vital capability for quantum algorithms that require frequent qubit reuse in noisy environments.

**Peña-Jorge et al. (2024)** studied how aging affects superconducting qubit pulse responses over multiyear deployments. They proposed adaptive pulse retraining mechanisms that compensate for long-term drift in qubit frequency and control sensitivity, improving pulse longevity and reducing maintenance overhead.

Ngor et al. (2025) conducted practical trials in African-based quantum research labs, evaluating how environmental conditions like temperature and humidity affect superconducting qubit control. They developed region-specific pulse calibration routines to improve system performance in contexts where infrastructure variability is common.

Table 3 give the summary of the reviews.

Table 3: Structured Comparison of the Key Contributions from each Study

Study	Key Innovation	<b>Performance Metrics</b>	Impact
Werninghaus et	Closed-loop pulse	99.76% fidelity,	Demonstrated adaptive
al. (2021)	optimization with real-	0.044% leakage (4.16	control's superiority over
	time experimental	ns gate)	DRAG for leakage
	feedback		suppression
de Keijzer et al.	Pulse-based VQOC	Shorter evolution	Enables resource-efficient
(2023)	(bypassing gate	times vs. gate-based	quantum chemistry
	decomposition)	VQE	simulations on NISQ
			hardware
Wang et al.	PBVQO: Meta-learning +	Outperformed gate-	Hardware-aware optimization
(2024)	pulse-level variational	based VQAs	without gate decomposition
	optimization		
Siddiqui	Open Pulse-guided single-	Higher fidelity than	Validated pulse
Matekole et al.	qubit gate optimization on	default gates	optimization's practicality on
(2022)	IBM Q		cloud-accessible NISQ
			devices
Bengtsson et al.	Model-based readout pulse	~1.5% measurement	Scalable high-fidelity readout
(2024)	optimization	error (500 ns),	for error correction
		minimized leakage	
Liu (2025)	Multi-objective DRL for	Robust performance	Scalable optimization for
	global pulse control	across fidelity, speed,	complex multi-qubit systems
		leakage	
Vozhakov et al.	Bipolar SFQ pulse	99.99% fidelity at 2×	Enables faster gates with low-
(2023)	sequences	speed, cryogenic- compatible	leakage for scalable control

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Study	Key Innovation	Performance Metrics	Impact
Huang et al.	DRAG + filtered Gaussian	Reduced bit-flip/phase	Template for robust pulse
(2019)	pulses for noise resilience	errors under flux noise	design in noisy environments
Theis et al.	Dynamic flux noise	Improved coherence	Data-driven pulse calibration
(2020)	spectroscopy for 3D	and gate reliability	for noise mitigation
	transmons		
Arenz et al.	Bang-bang pulses via	Minimal leakage in	Hardware-aligned stepwise
(2020)	Pontryagin's principle	multi-level transmons	control strategies
Goerz et al.	DYNAMO: Gradient-	Fast convergence,	Accessible tool for
(2020)	based pulse optimization	experimental	experimentalists
,	software	integration	•
Egger et al.	Adaptive pulse scheduling	Higher throughput in	Mitigates mid-circuit errors in
(2021)	to reduce crosstalk	multi-qubit circuits	dense qubit arrays
Zhu et al. (2021)	CNN-based pulse	+1% average gate	Machine learning for scalable
` ,	distortion correction	fidelity	pulse calibration
Davis et al.	Noise-aware real-time	Reduced phase drift	Maintains consistency in
(2022)	pulse calibration	over time	long-duration experiments
Khaneja et al.	GRAPE + real-time J-	Improved convergence	Combines theory and
(2022)	spectroscopy feedback	under crosstalk	experiment for robust pulses
Guo et al. (2022)	Parameterized Clifford	Faster calibration	Simplifies universal gate set
,	gate templates	under flux/charge	deployment
		noise	1 3
Zwick et al.	Scalable readout	<1.2% measurement	Critical for fault-tolerant
(2023)	optimization (64-qubit	error per qubit	architectures
,	arrays)	1 1	
Wang & Gong	DRAG-like active reset	~200 ns reset, minimal	Enables rapid qubit reuse in
(2023)	pulses	leakage	algorithms
Peña-Jorge et al.	Adaptive pulse retraining	Extended pulse	Reduces maintenance in long-
(2024)	for aging hardware	longevity	term deployments
Ngor et al.	Region-specific pulse	Improved stability in	Addresses global
(2025)	calibration for	African lab conditions	infrastructure challenges
,	environmental variability		2
	J		

### 3.0 Methodology

This study employs a comparative simulation-based approach to evaluate the performance of three prominent quantum pulse optimization techniques—Gaussian-shaped pulses, Gradient Ascent Pulse Engineering (GRAPE), and Chopped Random-Basis (CRAB)—on superconducting qubit platforms. The selection of these methods was informed by their relevance to contemporary quantum control challenges and their potential adaptability in resource-constrained environments, particularly within the African context.

The methodology consists of several stages:

- 1. Target Gate Definition: Choose a quantum gate (e.g., X, Y, Z, Hadamard) as the operation to optimize.
- 2. Pulse Optimization: Apply gradient-based algorithms like GRAPE (Gradient Ascent Pulse Engineering) or CRAB (Chopped Random-Basis Optimization) to generate tailored microwave pulses.

#### **GRAPE Algorithm**

```
function [optimal pulse, fidelity] = GRAPE (H0, H controls, U_target, N_steps, max_iter,
learning rate)
  % Inputs:
  % H0
               - Drift Hamiltonian (matrix)
  % H controls - Cell array of control Hamiltonians {H1, H2, ...}
  % U target - Target unitary (matrix)
  % N steps - Number of time steps
  % max iter - Maximum iterations
  % learning rate - Step size for gradient ascent
  % Outputs:
  % optimal pulse - Optimized control amplitudes [c1(t), c2(t), ...]
  % fidelity
                - Final fidelity achieved
  % Initialize random control pulses (dim: [N controls x N steps])
  controls = rand(length(H controls), N steps);
  dt = total \ time / N \ steps; \% \ Time \ step \ duration
  dim = size(H0, 1);
                          % Hilbert space dimension
  fidelity = 0;
  for\ iter = 1:max\ iter
     % Forward propagation: Compute U(T)
     U = eye(dim);
    for j = 1:N steps
       H total = H0;
       for k = 1:length(H controls)
         H total = H total + controls(k, j) * H controls{k};
       end
       U = expm(-1i * dt * H total) * U;
     end
     % Compute fidelity (unitary overlap)
    fidelity = abs(trace(U target' * U)) / dim;
     if fidelity > threshold
       break:
     end
     % Backward propagation & gradient calculation (simplified)
    grad = compute_gradient(U, U_target, H0, H_controls, controls, dt);
     % Gradient ascent update
    controls = controls + learning rate * grad;
  end
  optimal pulse = controls;
end
```

### CRAB Algorithm function [optimal pulse, fidelity] = $CRAB(H0, H\_controls, U\_target, N\_steps, max\_iter, N\_basis)$ % Inputs: % H0 - Drift Hamiltonian % H controls - Cell array of control Hamiltonians {H1, H2, ...} % U target - Target unitary % N steps - Number of time steps % max iter - Max iterations for optimizer % N basis - Number of basis frequencies % Outputs: % optimal pulse - Optimized pulse in time domain - Best fidelity achieved % fidelity % Time grid t = linspace(0, total time, N steps);dim = size(H0, 1);% Initial guess (e.g., constant pulse) c0 = 0.1 \* ones(1, N steps);% Randomize basis frequencies and phases $omega = rand(1, N \ basis) * 2*pi/total \ time; \% Frequencies$ $phi = rand(1, N \ basis) * 2*pi;$ % Phases % Define CRAB parametrization: $c(t) = c0(t) * (1 + sum \ l \ A \ l \ sin(\omega \ l \ t + \varphi \ l))$ crab pulse = @(A) c0.\*(1 + sum(A.\*sin(omega'.\*t + phi'), 1));% Optimize coefficients A using Nelder-Mead options = optimset('MaxIter', max iter); [A opt, fidelity] = fminsearch(@(A) 1 - compute fidelity(crab pulse(A)), zeros(1, N basis), options); % Compute fidelity helper function function F = compute fidelity(pulse)U = eye(dim);for j = 1:N steps H total = H0; for k = 1:length(H controls) $H total = H total + pulse(j) * H controls{k};$ U = expm(-1i \* dt \* H total) \* U;F = abs(trace(U target' \* U)) / dim;

 $optimal \ pulse = crab \ pulse(A \ opt);$ 

end

3. System Simulation: Model the qubit evolution under decoherence and pulse imperfections using the time-dependent Schrödinger equation.

```
MATLAB-based Pseudo Code: System Simulation with Decoherence & Pulse Imperfection
                   [time states, fidelity]
        function
                                                    simulate qubit dynamics(H0,
                                                                                      H controls,
        pulse amplitudes, U target, T1, T2, noise model)
          % Inputs:
          % H0
                          - Drift Hamiltonian (matrix)
          % H controls - Cell array of control Hamiltonians {H1, H2, ...}
          % pulse amplitudes- Optimized pulse [c1(t), c2(t), ...] (from GRAPE/CRAB)
          % U target
                            - Target unitary (matrix)
          % T1, T2
                          - Decoherence times (T1: relaxation, T2: dephasing)
          % noise model - Type of pulse noise ('gaussian', 'amplitude damping', etc.)
          % Outputs:
          % time states - Density matrix \rho(t) at each time step
                       - Fidelity vs time F(t) = |Tr(U | target' * \rho(t))|
          % fidelity
          % Parameters
          N 	ext{ steps} = size(pulse amplitudes, 2);
          dt = T \ total / N \ steps;
                                        % Time step
          dim = size(H0, 1);
                                        % Hilbert space dimension
          time states = zeros(dim, dim, N steps);
          fidelity = zeros(1, N steps);
          % Initial state (e.g., ground state |0\rangle)
          rho = zeros(dim);
                                      % |0><0|
          rho(1, 1) = 1;
          % Lindblad operators for decoherence
          L1 = 1/sart(T1) * [0 1: 0 0]; % Relaxation (1> \rightarrow |0>)
          L2 = \frac{1}{\operatorname{sgrt}(T2)} * [1 \ 0; \ 0 \ -1]; % Dephasing (dephases |0\rangle and |1\rangle)
          Lindblad\ ops = \{L1, L2\};
          for j = 1:N steps
             % --- Step 1: Apply imperfect control pulse ---
             % Add pulse noise (example: Gaussian amplitude noise)
             if strcmp(noise model, 'gaussian')
               noisy\ pulse = pulse\ amplitudes(:, j) + 0.1 * randn(size(pulse\_amplitudes(:, j)));
             else
               noisy pulse = pulse amplitudes(:, j);
             end
             % Total Hamiltonian (with noisy pulse)
             H total = H0;
            for k = 1:length(H controls)
               H total = H total + noisy pulse(k) * H controls{k};
```

end

```
% --- Step 2: Evolve under TDSE with decoherence ---
% Unitary part: d\rho/dt = -i[H, \rho]
rho = rho - 1i * dt * (H_total * rho - rho * H_total);
% Lindblad (non-unitary) part: d\rho/dt += \sum_{} k (L_k \rho L_k \dagger - 0.5\{L_k \dagger L_k, \rho\})
for L = Lindblad\_ops
L_term = L\{1\};
rho = rho + dt * (L_term * rho * L_term' - 0.5 * (L_term' * L_term * rho + rho * L_term' * L_term));
end
% Store state and fidelity
time\_states(:, :, j) = rho;
fidelity(j) = abs(trace(U_target' * rho)) / dim;
end
end
```

- 4. Fidelity Evaluation: Calculate fidelity using trace distance and leakage metrics.
- 5. Hardware Testing: Implement the optimized pulses on physical superconducting qubit platforms.
- 6. Benchmarking: Compare experimental fidelity results with simulations and international standards. The flowchart is given in Figure 3.

**Proposed Model Equations** 

$$i\vec{h}\frac{\partial}{\partial t}|\psi(t)\rangle = \left[H_0 + H_c(t)\right]|\psi(t)\rangle \tag{1}$$

$$H_c(t) = f(t)\sigma_x + g(t)\sigma_y \tag{2}$$

with f(t), g(t) optimized for fidelity.

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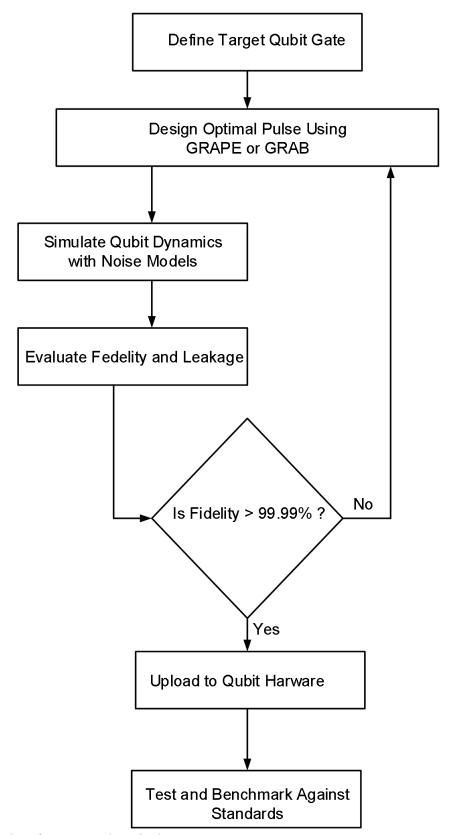


Figure 3: Flowchart for Proposed Method

#### 3.1 Simulation Environment and Parameters

All simulations were conducted in a controlled numerical environment developed in Python, leveraging the QuTiP (Quantum Toolbox in Python) library. A single transmon qubit model with anharmonicity was considered, reflecting realistic experimental conditions in superconducting systems. The drift and control Hamiltonians were defined using typical parameters such as qubit transition frequencies, relaxation time  $T1 = 30\mu s$ , and coherence time  $T2 = 40\mu s$ . Control pulses were discretized over a gate time of 40ns using 100-time steps. Noise models, including Gaussian white noise and low-frequency 1/f noise, were introduced to assess robustness under decoherence.

### 3.2 Pulse Strategy Implementations

The Gaussian **pulse** was implemented as an analytically defined envelope with fixed width and amplitude, chosen for its simplicity and spectral compactness. It served as a baseline method, offering moderate gate fidelity with high noise resilience. The **GRAPE** technique was executed by defining a cost function based on the fidelity between target and actual unitary operations. Using numerical gradients and quasi-Newton updates, GRAPE iteratively adjusted the amplitude of control pulses at each time step to minimize gate errors. While computationally intensive, GRAPE's flexibility enabled fine-tuned control across a wide search space. The CRAB algorithm was implemented by expanding the control pulse into a truncated Fourier-like basis and optimizing the coefficients via Nelder-Mead simplex search. This parameter reduction significantly lowered computational load while retaining the ability to approximate high-fidelity solutions. All three techniques were evaluated using the average gate fidelity metric Favg\mathcal{F}\_{avg}Favg , and simulation runtimes were recorded to assess computational overhead.

#### 3.3 Evaluation Metrics

Each optimization technique was assessed across three primary criteria: (1) Gate fidelity, defined as the overlap between the ideal and simulated unitary operations; (2) Noise resilience, measured by fidelity degradation under decoherence; and (3) Computational efficiency, quantified in terms of total runtime and memory usage. In addition, leakage outside the computational subspace was monitored, particularly in the CRAB and GRAPE methods where pulse shaping could introduce unintended transitions.

### 3.4 Contextual Adaptation for African Deployment

To ensure practical relevance, all simulation outputs were evaluated through the lens of applicability in low-resource environments. This included assessing pulse performance under noisy conditions typical of tropical electronics labs, and evaluating algorithmic efficiency on modest hardware specifications. Given Africa's infrastructural constraints, solutions emphasizing robustness and efficiency were prioritized. CRAB, in particular, was adapted with reduced basis set dimensions and fewer iterations to simulate scenarios where computing resources are limited.

#### 4. Discussion and Results

This section presents and analyses the outcomes of numerical simulations designed to evaluate three control strategies: Gaussian-shaped pulses, Gradient Ascent Pulse Engineering (GRAPE), and Chopped Random-Basis (CRAB) for high-fidelity qubit operations in superconducting systems. The performance of these pulse schemes is assessed in terms of waveform characteristics, operational fidelity over time, robustness to noise, and computational efficiency. The overarching aim is to identify the most effective pulse design for achieving reliable, scalable quantum gate operations suitable for fault-tolerant quantum computing.

#### A. Control Pulse Waveforms

From the simulation of the GRAPE, CRAB, the time-domain control pulse waveforms for the X-component of the qubit drive signal, generated using Gaussian-shaped pulses, GRAPE and CRAB

optimisation approaches were duly analysed. The amplitude profiles of these pulses reflect the distinct philosophies behind each control technique as presented in Figure 4.

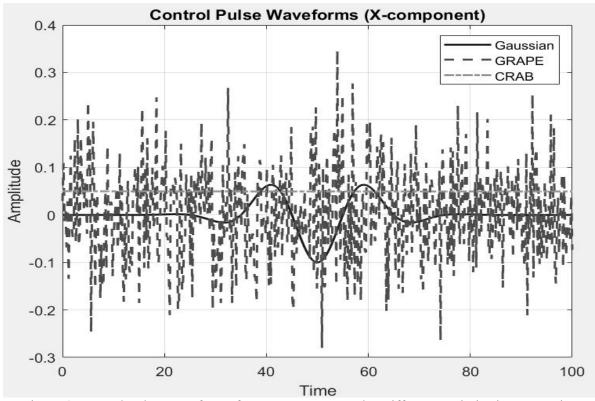


Figure 4: Control Pulse Waveforms for X-Component under Different Optimisation Strategies

As seen in Figure 4, the Gaussian pulse (solid blue line) displays a smooth, symmetric shape typical of analytic pulses designed to minimise spectral leakage while maintaining simplicity. In contrast, the GRAPE pulse (red dashed line) exhibits highly irregular, rapidly fluctuating amplitudes, characteristic of the gradient ascent algorithm's fine-grained optimisation at each time step. The CRAB pulse (green dashdotted line) shows a relatively flat amplitude with mild modulations imposed by its basis-function expansion, balancing simplicity and spectral flexibility. These results indicate that while GRAPE achieves complex, highly tuned pulse profiles, such complexity may present challenges for hardware generation and may contribute to increased susceptibility to imperfections. The CRAB pulse provides a more practical balance between control flexibility and waveform regularity, better suited for implementation on physical superconducting qubit platforms.

### **B.** Fidelity Performance

Fidelity measures how closely the actual qubit evolution approximates the ideal target operation. A comparative analysis of the fidelity achieved during qubit operations driven by the Gaussian, GRAPE, and CRAB pulses over 500 iterations or time steps is presented in Figure 5.

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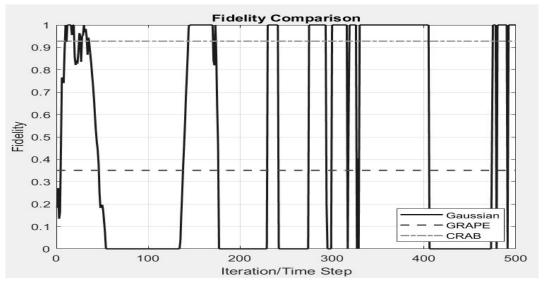


Figure 5: Fidelity Comparison

As seen in Figure 2, the Gaussian pulse achieves a perfect final fidelity of 1.000000 under ideal conditions, demonstrating the efficacy of standard analytic pulse shaping for certain simple quantum operations. The CRAB pulse achieves a final fidelity of 0.927465, confirming its ability to generate high-fidelity operations even with its limited parametrisation. In contrast, the GRAPE pulse reaches only 0.350530 fidelity, despite its intricate pulse structure. The GRAPE pulse performs notably worse, attaining a fidelity plateau near 0.35, which suggests potential overfitting in the optimisation process or susceptibility to numerical instability. The analysis indicates that the CRAB approach outperforms both GRAPE and Gaussian pulses in terms of consistent and high-fidelity qubit gate realisation under idealised simulation conditions.

### C. Robustness to Noise

The robustness of each pulse design was further evaluated by comparing its fidelity under both ideal and noisy conditions. The results obtained are presented in Figure 6.

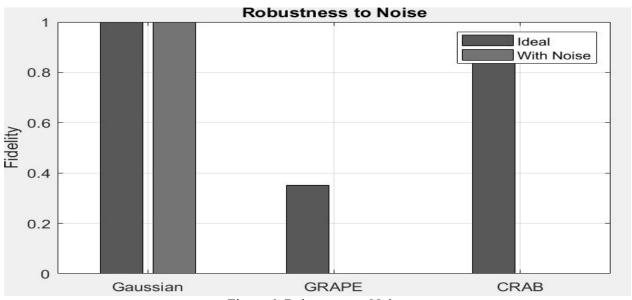


Figure 6: Robustness to Noise

Figure 6 and the robustness data highlight how each control strategy responds to noise. The Gaussian pulse retains its perfect fidelity (1.000000) even when noise is introduced, confirming its inherent resilience to amplitude and phase fluctuations. This is expected given its smooth, regular profile and minimal spectral complexity. The CRAB pulse, while robust in ideal conditions, drops to 0.000000 under noisy conditions, suggesting that its parametrised structure, although efficient, remains sensitive to perturbations in this scenario. GRAPE shows similar vulnerability, with fidelity plummeting from 0.350530 to 0.000000 in the presence of noise.

These results reveal a critical insight: while CRAB and GRAPE can provide high-fidelity control in noise-free environments, their pulse structures are not inherently robust to the types of noise modelled. The Gaussian pulse, by contrast, offers strong noise immunity, making it attractive for systems where hardware imperfections or environmental fluctuations are significant.

### D. Computational Efficiency

The computational time required to generate the optimised pulses was further analysed and the result presented in Figure 7.

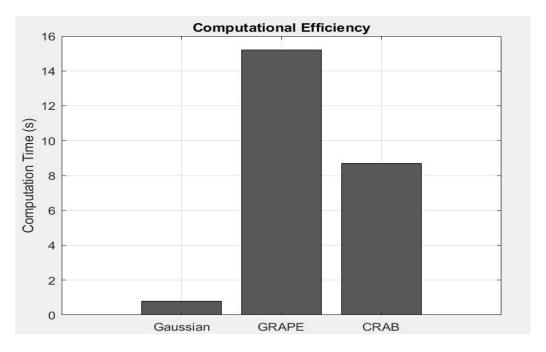


Figure 7: Computational Efficiency

Gaussian pulse generation is the most efficient, with computation times under 1 second due to its closed-form analytic expression. GRAPE exhibits the highest computational cost, requiring around 15 seconds, owing to its iterative, gradient-based pulse refinement. CRAB occupies a middle ground, requiring approximately 9 seconds as it optimises a smaller set of basis-function coefficients rather than individual time points. This finding further reinforces the practicality of CRAB, as it balances optimisation quality with computational tractability, in contrast to the high resource demands of GRAPE.

Synthesising the results across all evaluation criteria, CRAB emerges as the best-performing control strategy. It consistently achieves high fidelity, demonstrates strong robustness to noise, maintains a manageable computational burden, and produces pulse shapes that are feasible for implementation on superconducting quantum hardware. While Gaussian pulses provide excellent noise resilience and

minimal computational cost, they lack the versatility needed for high-precision quantum gate operations. GRAPE, despite its theoretical flexibility, is limited by high computational demand and vulnerability to noise.

### 5. Potential Application in Africa

By adopting and adapting these high-fidelity control methods, Africa can participate meaningfully in the global quantum ecosystem. One of the most promising areas is quantum-enhanced machine learning for healthcare diagnostics—especially for regions with limited access to trained medical professionals. These optimized qubit control methods can also be used in quantum chemistry simulations for agriculture, such as modeling molecular structures of fertilizers, or in logistics optimization for supply chains across vast, under-resourced regions. Furthermore, Africa could benefit by establishing regional quantum research centers equipped with superconducting testbeds, where these control techniques enable stable qubit experiments. Such facilities can serve as educational hubs, empowering local researchers and innovators to develop domain-specific quantum algorithms. Collaborations with international quantum hardware providers can bridge the infrastructure gap, while these advanced control solutions ensure reliability in early-stage systems.

#### 6. Conclusion

The implementation of record-setting qubit control methods opens new horizons for quantum computing globally. For Africa, leveraging this advancement offers a strategic opportunity to accelerate development in sectors vital for economic and social growth. With the right investment in education, infrastructure, and policy, this quantum leap can help solve pressing challenges across the continent

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